Mössbauer and heat capacity studies of ErZnSn₂

Abstract. Heat capacity results obtained for the intermetallic compound ErZnSn₂ were re-analysed to also consider, apart from the classical Debye model, the anharmonicity of the crystal lattice and the proper set of Einstein modes. The ¹¹⁹mSn Mössbauer technique was applied to derive the hyperfine interaction parameters characteristic of the two inequivalent crystallographic Sn sites in the compound studied. Quadrupole interaction constants, as measured by ¹¹⁹mSn Mössbauer spectroscopy, allowed for estimations of $V_{zz}$ components of the electric field gradient tensor that exist at both Sn sites in the discussed compound.

Keywords: ternary rare-earth intermetallics • heat capacity • Mössbauer spectroscopy

Introduction

Recently, new series of ternary intermetallics of the chemical formula RZnSn₂ (where R is substituted by the elements Y, Gd, Tb, Dy, Ho, Er, Tm, or Lu) were successfully synthesized. X-ray diffraction investigations showed that their crystalline structure is of a tetragonal HfCuSi₂ type [1]. These compounds belong to the broad group of R(A)-T-X (where R stands for a rare-earth or A – actinide element, T is a d metal, and X is a p element) ternary intermetallics [2–21], which display numerous crystalline and magnetic structures and a wealth of intriguing physical properties like complex magnetic orderings, unconventional superconductivity or fluctuating valence. Magnetic susceptibility together with heat capacity results show that the compound LuZnSn₂ does not undergo any magnetic phase transitions at temperatures as low as 1.9 K [1, 22], and therefore this compound is an ideal reference material for the estimation of magnetic contributions to the heat capacity of magnetically ordered isostructural compounds, for example ErZnSn₂ that shows a clear phase transition within the experimental temperature range between paramagnetic and antiferromagnetic states with a Néel temperature $T_N = 5.0$ K [1]. Additionally, the antiferromagnetic character of the latter compound was corroborated by the observed negative value of its paramagnetic Curie temperature $\theta_p = -8.8$ K as well as by the metamagnetic behaviour of the recorded magnetization curve measured at the lowest temperatures [1]. It is worth noting that the obtained effective magnetic moment, $\mu_{\text{eff}} = 10.47 \mu_B$, is remarkably higher than the expected theoretical value characteristic of the
Er\textsuperscript{3+} free-ion value \( \mu_{\text{eff}} \text{(theor.)} = g \mu_B [J(J+1)]^{1/2} = 9.58 \mu_B \). The observed excess of effective magnetic moment has already been discussed [1], and might be interpreted as the contribution originating from the d-electrons of Zn.

The main purpose of this report is to present and discuss a new analysis of heat capacity data [22] obtained for ErZnSn\textsubscript{2} with the help of an extended Debye model that fits experimental data over the whole range of temperatures, in contrast to previous results [22] where a simple Debye model was used. Additionally, the results of a Mössbauer investigation conducted at room temperature with a \(^{119}\text{Sn}\) source is reported and discussed with regard to the compound studied.

**Experimental**

The polycrystalline ErZnSn\textsubscript{2} sample was prepared, as previously described [1], by melting the constituent elements at \(-1000^\circ\text{C}\) followed by an annealing procedure at 400\(^\circ\text{C}\). Its crystal structure was derived from an X-ray powder diffraction pattern by means of the Rietveld method using the FullProf program package [23] (see reference [1]).

Magnetic and heat capacity measurements were carried out for the bulk sample within the temperature range from 1.9 K to 300 K using a vibrating sample magnetometer (VSM) and the heat capacity (HC) insert of the Quantum Design Physical Property Measurement System (PPMS). The reported specific heat studies were performed in a zero external magnetic field. It must be stressed that great care was taken to properly correct the obtained raw HC data by accounting for the specific heat contribution originating from the supporting platform and the adhesive Apiezon N addenda applied to couple our sample to the PPMS HC platform. For this purpose the HC curve of the supporting platform plus an appropriate amount of adhesive addenda (about 0.2 mg) was pre-measured and subtracted from the raw HC data.

The \(^{119}\text{Sn}\) Mössbauer spectrum was measured in transmission geometry at room temperature by means of an electromechanical spectrometer of Kankeleit type operating in the constant-acceleration mode utilizing a \(^{119}\text{Sn}\) source in the CaSnO\textsubscript{3} matrix. A proportional counter was used to detect the incoming 23.875 keV \( \gamma \)-rays. The routine calibration of the velocity scale was conducted at room temperature using a standard \(^{57}\text{Co}\) (Rh) source and a metallic iron foil. The obtained resonance absorption spectrum of \(^{119}\text{Sn}\) was fitted by means of the least-squares fitting procedure within the transmission integral taking into account the full hyperfine Hamiltonian interaction for calculations of the resonance-line positions and their relative line intensities.

**Results and discussion**

**X-ray diffraction**

The analysis of the recorded X-ray diffractogram confirms that the ErZnSn\textsubscript{2} compound crystalizes in a similar way to the tetragonal structure of HfCuSi\textsubscript{2} (P\textsubscript{4}/nmm space group). Two symmetrically inequivalent Sn sites, 2\(a\)(4\(-m\)\(_2\)) and 2\(c\)(4\(mm\)) exist in the unit cell and exhibit a 1:1 nominal occupational ratio [1].

**Heat capacity**

The measured specific heat capacity data are displayed in Figs. 1a and 1b. A sharp \( \lambda \) type anomaly for ErZnSn\textsubscript{2} was recorded at \( T_N = 5.0 \text{ K} \) in perfect agreement with the Néel temperature determined from the magnetic measurements taken under the influence of a low external magnetic field [1]. The magnetic contribution, \( C_{\text{magn}} \), for the compound ErZnSn\textsubscript{2} can be separated from its total specific heat capacity, \( C_p \), using the following equation:

\[
C_p = C_{\text{lat}} + C_{\text{magn}}
\]

where \( C_{\text{lat}} \) is the sum of the conduction electron \( C_e = \gamma T \) and the phonon part \( C_{\text{ph}} \), i.e. the lattice contribution to the total specific heat capacity. Bearing in mind that \( C_p(T) \) curves measured for Er and Lu intermetallics overlap in a good approximation at

![Fig. 1. Temperature dependencies of the specific heat capacity (C\(_p\)) for ErZnSn\(_2\) together with fitted C\(_p\) lattice contribution (as explained in the text) (a) and C\(_{\text{magn}}\)/T (b) where C\(_{\text{magn}}\) was obtained by subtracting the fitted C\(_p\) lattice curve (i.e. the curve in red, Fig. 1a) or the \( C_p \) for the non-magnetic reference material, i.e. LuZnSn\(_2\) (continuous line in black, Fig. 1b). The derived fitting parameters are gathered in Table 1.](image-url)
Table 1. The results for the derived fitting parameters from specific heat capacity data obtained for ErZnSn2 using Eq. (1)

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Multiplicity $m_i$</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\theta_0$</td>
<td>$(141.78 \pm 0.34)$ K</td>
<td>–</td>
<td>settled as for LuZnSn2 [24]</td>
</tr>
<tr>
<td>$\theta_1$</td>
<td>$(56.38 \pm 0.11)$ K</td>
<td>$\times 1$</td>
<td>settled as for LuZnSn2 [24]</td>
</tr>
<tr>
<td>$\theta_2$</td>
<td>$(148.51 \pm 0.71)$ K</td>
<td>$\times 5$</td>
<td>fitted</td>
</tr>
<tr>
<td>$\theta_3$</td>
<td>$(262.30 \pm 1.60)$ K</td>
<td>$\times 3$</td>
<td>fitted</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>$(12.79 \pm 0.26) \times 10^{-5}$ K$^{-1}$</td>
<td>–</td>
<td>fitted</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>$(5.28 \pm 0.05) \times 10^{-3}$ J·mol$^{-1}$·K$^{-2}$</td>
<td>–</td>
<td>settled as for LuZnSn2 [24]</td>
</tr>
</tbody>
</table>

temperatures above ~50 K [22], one can choose the compound LuZnSn2 as a good reference material making the rough estimation of $C_{lat}$ for ErZnSn2 and for other magnetic members of the RZnSn2 series possible. Therefore, it is obvious that by subtracting both curves the $C_{\text{magn}}(T)$ value for the Er compound can be calculated. In turn, integration of $C_{\text{magn}}(T)/T$ yields the magnetic entropy contribution, $S_{\text{magn}}$, amounting to 15.62 J/(mol·K) (or 14.90 J/(mol·K) when the fitted curve in red is used) as shown in Fig. 1b, which is less than the value $R\ln16 = 23.05$ J/(mol·K) expected for the ground state $f = 15/2$ multiplet of Er$^{3+}$.

It is worth mentioning that the simple formula for $C_{lat}$:

\[
C_{lat} = C_{el} + C_{ph} = \gamma T + C_{ph}
\]

where $C_{ph}$ is described by the classical Debye formula:

\[
C_{ph} = 9R \left( \frac{T}{\theta_D} \right)^3 \int_0^{\theta_D} \frac{x^4 e^x}{(e^x - 1)^2} dx
\]

is not suitable for the fitting of $C_p(T)$ dependencies measured for the intermetallics Y and Lu including that for Er far above $T_N$ [22]. However, it was shown that the experimental heat capacity data, $C_{lat}(T)$, for LuZnSn2 [24] and ErZnSn2, as expounded in this work, can be successfully fitted over the whole temperature range by taking into account anharmonic effects that occur at elevated temperatures, as well as by the inclusion of selected Einstein modes for LuZnSn2 and ErZnSn2 respectively using the extended Debye equation in the form:

\[
C_p = C_{ph,el} = 9R \left( \frac{T}{\theta_D} \right)^3 \int_0^{\theta_D} \frac{x^4 e^x}{(e^x - 1)^2} dx + R \frac{1}{1 - \alpha T} \sum_i m_i \left( \frac{\theta_{E_i}}{T} \right)^2 e^{\nu_{i}/T} + \gamma T
\]

The point symmetries of Sn environments, i.e. $\bar{4}m2$ (2a site) and $4mm$ (2c site), ensure non-zero values of the axially symmetric (with asymmetry parameter $\eta = 0$) electric field gradient (EFG) tensor at these sites, and as a consequence, non-zero electric quadrupole hyperfine interaction parameters at both Sn positions in the ErZnSn2 lattice. In accordance with the two non-cubic environments of Sn atoms in the crystal structure, i.e. 2a and 2c sites, the spectrum recorded at room temperature can be reasonably fitted with two quadrupole-split components including a single line of the metallic impurity tin (with isomer shift $\delta_{is}$ kept constant and equal to 2.552(9) mm/s [25]), which is also evident from X-ray diffraction analysis and originates from the synthesis procedure as well as the known decomposition process of the probe over time. Similarly to the case of LuZnSn2 [24], the resonance spectrum recorded for ErZnSn2 at room temperature can be fitted with different pairs of main quadrupole split subsets of hyperfine parameters (together with the respective pairs of isomer shifts) for two crystallographically inequivalent Sn sites. However, from a physical point of view, a fit with only two different quadrupole interaction constants and comparable isomer shifts for both Sn sites (Fig. 2) is acceptable. One can underline here that such a situation is observed in the closely

![Fig. 2. $^{119}$Sn Mössbauer spectrum of ErZnSn2 at room temperature fitted with two quadrupole doublets and one strictly settled single line metallic tin impurity component (see text for explanation).](image-url)
related series of defected GdT$_2$Sn$_2$ compounds [21], where Sn atoms also occupy two different symmetry positions and where Mössbauer spectra can be fitted in a suitable way with only two different quadrupole splittings, but with very similar isomer shifts for both Sn sites. On the other hand, an assumption that isomer shifts should be significantly different at Sn sites seems to also be unreasonable, since for Sn atoms their transformation requires a rather big change in the valence electron sp configuration of their own tin atoms [24], and this is not expected here, as in the 2a position Sn atoms interact directly with the other four Sn and Er atoms, respectively, while at the 2c site Sn atoms interact with four Zn (instead of Sn) and Er atoms, respectively, but valence electron s configurations of Sn and Zn atoms remain roughly identical. The observed systematics of the isomer shifts of Sn in most intermetallic systems (including ternary systems) [26] is in line with the previous statement, showing that the effective number of 5s tin electrons is merely the same and not much different than one (see Table 9a in [26]). In this context, one can state that a theoretical support in predicting Mössbauer parameters would be of great importance. In particular, the theoretical calculations could enable the right association of the obtained sets of experimental results for hyperfine parameters for a given site in the crystallographic structure and also facilitate the correct interpretation of the derived isomer shifts and quadrupole splittings, giving a deeper insight into the electronic structure of the studied material. In this regard one can only speculate, for example, that a larger quadrupole splitting could be associated with a lower symmetry site of Sn. Nowadays, the application of density functional theory (DFT) is quite successful in this regard, but to the best of our knowledge such calculations were not made for Sn hyperfine parameters in the system studied.

Generally, to obtain reliable results from a given fitting procedure, some parameters, like half-widths for source $\Gamma_s$ and absorber $\Gamma_a$, have to be constrained and kept constant, being equal to those derived from earlier experiments with reference to the absorber BaSnO$_3$. In this case these values are as follows: $\Gamma_s = 0.37$ mm/s and $\Gamma_a = 0.35$ mm/s. Additionally, only fits with comparable relative intensities for both quadrupole components were acceptable to reflect the fact that the occupation of the above-mentioned Sn sites is equal. It must be stressed, that fits with constrained amplitudes of main Sn contributions with their 1:1 ratio, do not remarkably change the goodness, $\chi^2$, of such a fit. Small differences between relative intensities can always be explained by possible differences in Debye-Waller f factors for both symmetry sites of tin. This is the main reason why in Table 2 the derived Mössbauer results are presented for fits with unconstrained main Sn contributions. The subtraction of the sum of the derived intensities for both quadrupole components from 100% yields the contribution of the Sn impurity being equal to about 5.5% (see Table 2). The required values of the electric field gradient $V_{zz}$ at the tin nuclei can be obtained using the quadrupole interaction constants $\Delta E_Q = eQV_{zz}$ (where the nuclear quadrupole moment $Q$ for the first excited state of $^{119m}$Sn is equal to $\sim 0.094b$ [27]) given in Table 2 by the simple relation: $V_{zz} = -8.47128 \times 10^{20} \times \Delta E_Q$ [mm/s] V/m$^2$ and they are $|V_{zz}| = 25.6 \times 10^{20}$ V/m$^2$ and $|V_{zz}| = 13.8 \times 10^{20}$ V/m$^2$, respectively.

**Conclusions**

It was shown here that the experimental specific heat capacity data, $C_p(T)$, for ErZnSn$_4$ can be successfully fitted over the whole temperature range using an extended Debye model which takes into account the effect of lattice anharmonicity and the suitable number of Einstein modes. Mössbauer spectra can be fitted in a suitable way with only two different quadrupole splittings, but with almost the same isomer shifts for both Sn sites.

Those obtained by $^{119m}$Sn Mössbauer spectrocopy quadrupole interaction constants enabled the determination of very important $V_{zz}$ components of electric field gradient (EFG) tensors at both Sn sites of ErZnSn$_4$ in the field of solid-state physics. The derived isomer shifts of about 2.19 mm/s are characteristic of tin in metallic systems.

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**References**


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**Table 2. Hyperfine interaction parameters inferred from the $^{119m}$Sn resonance spectrum obtained for the intermetallic compound ErZnSn$_4$ at 293 K**

| Component | $\delta_{ss}$ [mm/s] | $|\Delta E_Q|^\circ$ [mm/s] | Relative area [%] | $\chi^2$ |
|-----------|---------------------|---------------------------|------------------|---------|
| I         | 2.185(3)            | 3.019(24)                 | 45.2(1.2)        | 1.1575  |
| II        | 2.186(3)            | 1.634(20)                 | 49.3(1.3)        |         |


